

Magnesium Fluctuations Modulate RNA Dynamics in the SAM-I Riboswitch

Ryan L. Hayes,[†] Jeffrey K. Noel,[†] Udayan Mohanty,[‡] Paul C. Whitford,[†] Scott P. Hennelly,[§]
José N. Onuchic,[†] and Karissa Y. Sanbonmatsu^{*,§}

[†]Center for Theoretical Biological Physics and Department of Physics & Astronomy, Rice University, Houston, Texas 77005-1892, United States

[‡]Department of Chemistry, Boston College, Chestnut Hill, Massachusetts 02467, United States

[§]Theoretical Biology and Biophysics, Theoretical Division, Los Alamos National Laboratories, Los Alamos, New Mexico 87545, United States

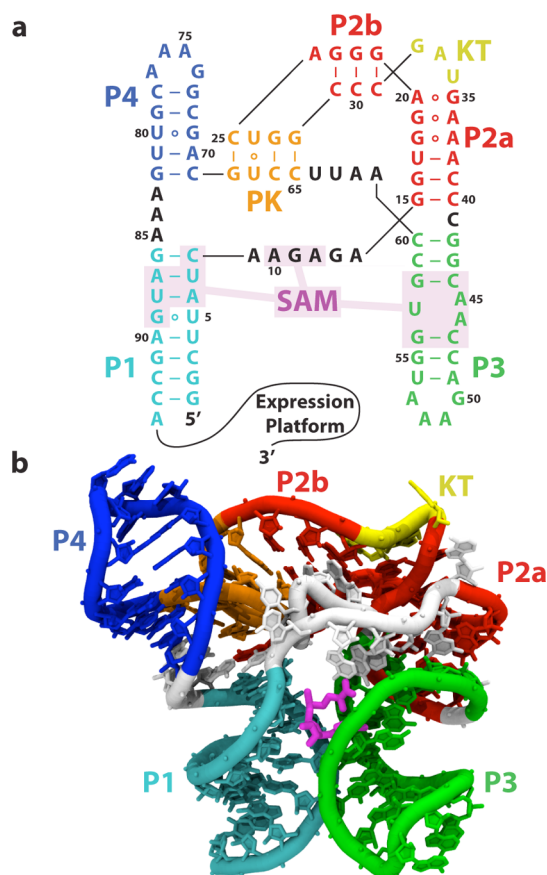


Figure 1. SAM-I riboswitch aptamer domain. (a) The secondary structure with the SAM binding pocket (nucleotides within 5 Å of SAM) shaded. Nucleotides are color-coded according to secondary structure element. Helices P1, P2a, P2b, P3, and P4 are labeled, along with the kink-turn (KT) and pseudoknot (PK). (b) The crystallographic structure of the SAM-I riboswitch aptamer domain solved by Batey and co-workers, colored using the same color scheme as (a). Magenta, SAM ligand.

key player in sulfur metabolism (Figure 1). In the absence of SAM, a long terminator helix is formed, which causes transcriptional termination. In the presence of SAM, a compact aptamer is formed at the expense of the terminator helix, allowing gene expression to proceed.¹⁶ As one of the first riboswitches discovered, the SAM-I riboswitch is well studied and is an excellent model system.¹⁷ In this work, we use SAM-I to examine the effect of the ionic environment, and specifically Mg^{2+} , on RNA.

RNA is strongly charged, so the ionic environment is of crucial importance in attenuating electrostatic repulsion as the tertiary structure of RNA packs it into a small volume.^{9,10} In order to balance its strong negative charge and maintain electroneutrality, RNA attracts positive ions out of bulk solution and repels negative ions. The number of excess ions an RNA molecule attracts into its local environment is called the preferential interaction coefficient (Γ_i) for a species i , and depends strongly on available ionic concentrations.¹⁸ Local enrichment of Mg^{2+} and K^+ , and a local depletion of anions, are responsible for balancing most of the RNA charge.

Mg^{2+} is especially important because RNA rarely forms tertiary structure in the absence of Mg^{2+} .¹⁰ First, it is entropically cheaper to balance the charge with divalent Mg^{2+} because it requires only half as many condensed ions as

monovalent ions to balance the charge. Furthermore, since Mg^{2+} is divalent, it can attract multiple phosphates at once, which results in attractive bridging interactions between what would otherwise be repulsive phosphates.^{19,20} Lastly, due to its small size, Mg^{2+} is able to get closer to RNA, which enables it to outcompete other divalent ions.^{21,22}

The treatment of ions in theoretical models of RNA is an active area of research. Continuum approximations range from Debye–Hückel²³ to more sophisticated nonlinear Poisson–Boltzmann (NLPB) approaches.^{24–26} These reduced description treatments are necessary in implicit solvent simulations or when atomistic calculations are impractical. Since these models treat the ionic environment as a continuum, molecular details of the ionic environment are necessarily lost, including ion–ion correlations and discrete ion effects.⁶ The importance of these discrete ion effects on the molecules with which they interact is an open question. In Manning counterion condensation theory, when the linear charge density of a polyelectrolyte chain is high enough, as it normally is in RNA, ions condense from aqueous solution to shield the phosphate backbone, effectively renormalizing its charge.²⁷ If the distance between these Manning condensed counterions is less than or equal to the Debye screening length (both are approximately 6.5 Å in our simulations), these counterions strongly interact with each other and behave as a strongly correlated ionic liquid or glass.²⁸

Here we carefully examine the interaction between RNA and its ionic environment through MD simulations. We observe a previously underappreciated class of transient, outer-sphere coordinated Mg^{2+} with glassy dynamics, which couples to and modulates RNA kinetics. Outer-sphere ions are by far the largest group observed in our simulations (80%), and the focus of this paper. This class of Mg^{2+} is poorly represented by the continuum approaches we have outlined. While the thermodynamics of this class are captured with varying degrees of accuracy, these models are incapable of capturing the rich internal dynamics or the control over RNA kinetics by outer-sphere Mg^{2+} .

Outer-sphere Mg^{2+} ions comprise one of four regimes of Mg^{2+} behavior we observe in our simulations. These regimes are largely delineated by the distance from the RNA, and are divided into the following classes: inner-sphere, outer-sphere, diffuse, and free. *Inner-sphere* ions, which include chelated ions as a subset, shed part of their hydration shell and bind directly to the RNA via inner-sphere contacts. *Outer-sphere* ions are coordinated with the RNA via outer-sphere contacts, and interact through a single hydration shell. *Diffuse* ions have multiple hydration shells and are poorly ordered, but are enriched above bulk concentration. Beyond the diffuse ions are the *free* ions, where the enrichment of ions ceases and the RNA charge has been screened out.

Our results show that outer-sphere Mg^{2+} local density fluctuations, residence times, and RNA fluctuations occupy similar time scales and kinetically couple. We observe that Mg^{2+} alters RNA kinetics in two ways. First, increased Mg^{2+} concentration tends to slow the kinetics of RNA fluctuations, and second, local Mg^{2+} density changes due to individual ion association events are correlated with RNA conformation. In order to better understand Mg^{2+} interactions, we characterize the behavior of Mg^{2+} in the presence of RNA. The Mg^{2+} distribution is controlled by electronegative RNA atoms, hydration shells, and a preference for the major groove. The differing distance classes of Mg^{2+} have different diffusive behavior, and careful analysis of the diffusion data suggests that

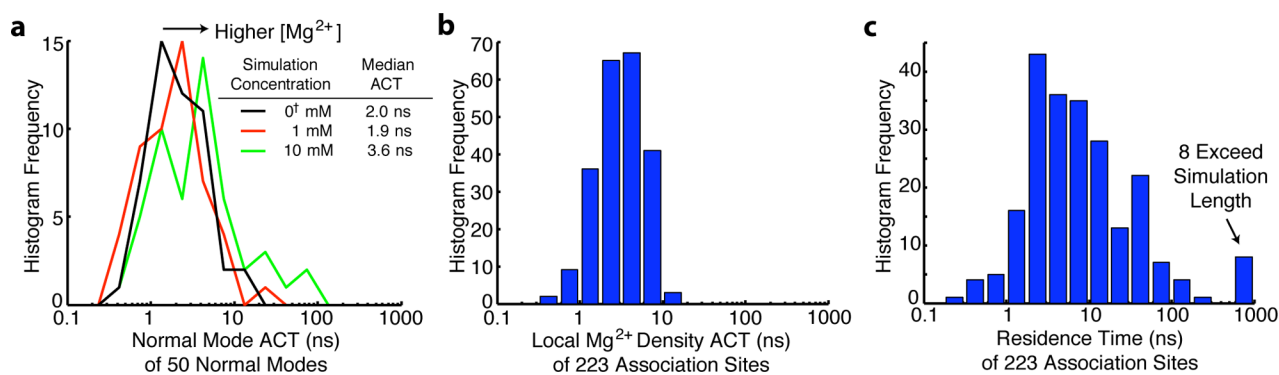


Figure 2. Mg^{2+} affects RNA kinetics. (a) The distribution of autocorrelation times (ACTs) for the MD trajectories projected onto the lowest 50 normal modes. The time scales of RNA fluctuations increase with Mg^{2+} concentration in accordance with experiment. This occurs because Mg^{2+} tightens RNA tertiary contacts and stabilizes compact conformations. (b) The distribution of ACTs for the local Mg^{2+} density around several association sites. The time scales of RNA fluctuations are comparable to the time scale of the RNA fluctuations, which allows them to kinetically couple. (c) The residence time for the association sites.

the outer-sphere Mg^{2+} near RNA behaves like a supercooled strong ionic liquid. Because outer-sphere Mg^{2+} ions account for 80% of excess Mg^{2+} in our simulations, and because of their rich dynamics, they may change the paradigm of Mg^{2+} –RNA interactions. Rather than a few inner-sphere ions anchoring the RNA structure surrounded by a continuum of diffuse ions, our results reveal a layer of outer-sphere coordinated Mg^{2+} strongly coupled to the RNA.

2. MODEL AND METHODS

2.1. Simulation Details. MD simulations of the SAM-I riboswitch were performed with and without SAM in the presence of five varying Mg^{2+} concentrations. Individual simulations were 2 μs , for a total of 20 μs of sampling. Simulations were carried out using the Gromacs v4.5.1 MD package.²⁹ The Amber 99 forcefield³⁰ was used, with modified K^+ ion parameters and SPC/E water to prevent crystal formation.^{31,32} Because of its importance for stability, we parametrized the SAM metabolite for AMBER. In order to parametrize the SAM, we used GAMESS quantum mechanics software³³ and the RED software package³⁴ to compute the charges on each atom using the Restrained ElectroStatic Potential method.^{35,36} The remaining forcefield parameters were taken from the Generalized Amber ForceField.³⁷ Simulations were run with a time step of 2 fs, and bond lengths for hydrogen atoms were fixed using LINCS.³⁸ Particle mesh Ewald electrostatics³⁹ were used with an Ewald radius of 15 Å and a van der Waals cutoff of 15 Å.

Since the maximum linear dimension of the SAM-I aptamer is 70.7 Å, a water box of 100 Å was used to allow a careful examination of the ionic environment. Simulations contained approximately 98 000 atoms. The simulations had target concentrations of 100 mM KCl, and 0, 0⁺, 1, 6, and 10 mM MgCl_2 in bulk. The 0 mM Mg^{2+} simulation contained no Mg^{2+} ions, while the 0⁺ simulation contained a single poorly resolved Mg^{2+} ion taken from the crystal structure (near A10 and U64) which we predict to be chelated (see below for details). The presence of a Mg^{2+} near this predicted chelation site has been suggested to be important for stability.^{4,40} This ion was included in all remaining simulations. Since the RNA is strongly charged, it balances this charge by attracting Mg^{2+} and K^+ ions into and repelling Cl^- ions from its local environment. These excess ions do not count toward the bulk concentration. Therefore, the ions in a simulation are a combination of excess ions which balance the RNA charge and bulk ions. The number of excess ions is equal to the preferential interaction coefficient. Each bulk ion contributes 1.7 mM for our box size. Since preferential interaction coefficients vary with concentration, several preliminary equilibrations were run to determine the correct number of ions to include so that the desired concentrations would remain in bulk. For example, in the 10 mM simulation, the predicted chelated ion and 32 hydrated Mg^{2+} ions were included, but 27 of these were

excess ions, and only 6 contributed to the bulk concentration. See Table 1 for more details.

2.2. Equilibration. Equilibration began from the crystal structure (Protein Data Bank accession code 2GIS¹⁶), using our well-established protocol.^{41,42} The RNA was frozen and placed in a waterless box. Ions were placed randomly with larger van der Waals radii to prevent them from condensing onto the RNA without an appropriate hydration shell. For the sole purpose of establishing the starting configuration of ions for explicit solvent simulations, the ions were equilibrated using stochastic dynamics and a dielectric constant of 80 to mimic water for 10 ns until the electrostatic energy converged. Water was then added to the box, and annealed to 300 K over 200 ps with the RNA and ions frozen. The ions were released and allowed to equilibrate at constant volume for 2 ns. The RNA was then gradually released over 10 ns, spending 2 ns each with position restraints of 1000, 100, 10, 1, and 0 kcal/mol/nm², at constant pressure. This amounted to 10 ns of waterless equilibration followed by 12.2 ns of explicit solvent equilibration. From this point on, unrestrained explicit solvent simulations were performed, including explicit solvent and explicit ions with full particle mesh Ewald electrostatics.

Upon the addition of water, the bulk concentration and the radial distribution functions of the K^+ and Cl^- ions converged quickly, on a time scale of approximately 0.5 ns. The K^+ distribution function changed due to a few K^+ ions partially shedding their hydration shells, which was not allowed before the addition of water. Since the equilibration was much longer than 0.5 ns, K^+ and Cl^- were well equilibrated. Post-simulation analysis of relevant time scales (see section 3.1.2) validated that equilibration was reasonable for Mg^{2+} as well. While some Mg^{2+} sites had association times in excess of the simulation time, the largest density fluctuation times for Mg^{2+} of these sites were approximately 20 ns, and bulk Mg^{2+} concentration fluctuated with a time scale between 5 and 8 ns, depending on the Mg^{2+} abundance. These time scales are all less than or comparable to the 12.2 ns of explicit solvent equilibration. Thus, this equilibration procedure allowed the RNA to equilibrate with the ionic environment while keeping it close to the crystal structure.

3. RESULTS AND DISCUSSION

In section 3.1, the simulations of the SAM-I riboswitch show that outer-sphere Mg^{2+} and RNA fluctuate on the same time scales and couple. Both collective effects (the bulk concentration of Mg^{2+}) and local effects (individual Mg^{2+} association events) affect RNA dynamics. In section 3.2, characterization of the Mg^{2+} diffusion and distribution reveals molecular mechanisms by which Mg^{2+} influences RNA: a layer of Mg^{2+} ions separated from the RNA by a single hydration layer constitutes the majority of the excess ions ($\Gamma_{\text{Mg}^{2+}}$). Ions in this

layer are positioned by electronegative RNA atoms, hydrations shells, and a preference for the major groove.

3.1. Mg^{2+} –RNA interactions and Time Scales.

3.1.1. Global RNA Dynamics. In our simulations, the Mg^{2+} concentration has a measurable effect on global fluctuations (Figure 2a). To characterize the global dynamics of the RNA, global coordinates are needed. The explicit solvent MD simulation trajectories were projected onto normal modes.^{43–45} In this context, normal-mode analysis is advantageous relative to principal component analysis⁴⁶ because normal-mode analysis produces a consistent measure between all simulations (see SI for more details). A structure-based potential^{47,48} was used to compute normal modes, rather than the typical Tirion potential.⁴⁹ This is the first time this potential has been used for normal modes to our knowledge.

In order to determine time scales of RNA motion, trajectories were projected onto the first 50 normal modes. After subtracting a linear fit to remove drift along unstable normal modes, autocorrelations were computed as a function of time (SI, eq S2). The autocorrelations generally had long nonexponential tails, suggesting the presence of multiple time scales. This is to be expected because processes in RNA range over many orders of magnitude, up to the ligand dissociation time scale, which is too slow to observe in the simulations. To obtain the dominant time scale for each normal mode, the time when the autocorrelation fell below $1/e$ was taken. This dominant time scale represents the duration of the largest structural changes that occur within the 2 μs simulation. The peak of the distribution of times changes with Mg^{2+} concentration. The median time scale of the autocorrelations increased from 2.03 ns for 0⁺ mM Mg^{2+} to 3.55 ns for 10 mM Mg^{2+} , showing that increasing Mg^{2+} concentration slows structural fluctuations.

It has been shown that while Mg^{2+} is much more effective than K^+ at stabilizing RNA, Mg^{2+} also tends to slow transition rates by reducing the entropy of transition-state ensembles.^{19,50} The observed lengthening of autocorrelation time scales for RNA fluctuations in the presence of Mg^{2+} provides a mechanism for such a slowing in the presence of Mg^{2+} . The Mg^{2+} stabilizes the compact structure, so the RNA must wait longer before a sufficiently large fluctuation occurs to induce a transition.

3.1.2. Local Mg^{2+} Dynamics. Before it is possible to quantify the effects of individual Mg^{2+} association events on RNA, it is necessary to identify sites where Mg^{2+} associates with RNA. Association sites were identified by finding the average position of a Mg^{2+} ion with respect to the RNA between times when its diffusion fell below 10 $\mu\text{m}^2/\text{s}$ and rose back above 100 $\mu\text{m}^2/\text{s}$. (The experimental diffusion of aqueous MgCl_2 is 1100 $\mu\text{m}^2/\text{s}$.) Diffusion as a function of time was computed by fitting $\langle x^2 \rangle = 6Dt$ to the mean-squared deviation of Mg^{2+} positions (fitted to the RNA structure). We identified 223 sites where Mg^{2+} associates with RNA. Mg^{2+} dwell times in these sites ranged from a few to several hundred nanoseconds.

To quantify Mg^{2+} association with RNA, Mg^{2+} density near these association sites was computed as a function of time by counting the number of Mg^{2+} within a cutoff distance of the site. The cutoff used was typically 10 Å, which is large enough to accommodate two or three Mg^{2+} , but values of 8, 6, and 4 Å were also tried with similar results. This density measure showed whether an association site was effectively occupied or unoccupied at any given time.

In order to determine the time scales of local Mg^{2+} density fluctuations, autocorrelations of the local Mg^{2+} density time traces were computed (eq S2). Most (approximately 85%) of the local density autocorrelations were generally exponential. Characteristic times were taken from when the autocorrelation crossed $1/e$, and binned (Figure 2b). Nearly all sites have fluctuation times between 1 and 10 ns. A site may tend to be occupied for much longer, but in that case the fluctuation times correspond to transient periods when the site is empty, and these unoccupied times are generally less than 10 ns. Shell sizes other than 10 Å give comparable time scales (Figure S2), even though a 4 Å shell just captures if a Mg^{2+} is in that site, and 10 Å captures a broader picture of the local density.

Since residence times need not correspond with local Mg^{2+} density fluctuation times, it is informative to examine residence times as well. To determine residence times for each site, a modified autocorrelation approach was used. For each site and each Mg^{2+} , a time-dependent boolean variable was assigned to 1 if the Mg^{2+} ion was within 4 Å of the association site, and 0 otherwise; 4 Å was chosen to ensure only ions in that association site were considered associated, rather than ions in neighboring sites or more transient ions which might come within 10 Å. This boolean variable was then autocorrelated without subtracting the mean. These autocorrelations represent how long the same ion remains associated rather than how long a density fluctuation from the mean lasts. For each association site, the averages in (eq S2) were taken over time and over all Mg^{2+} ions. Due to the noisy tails of the autocorrelation functions, residence times were taken from when autocorrelations fell below $1/e$.

Residence times occupy a much broader range, including eight that are longer than the simulation time (Figure 2c). Residence times correlate well with the 4 Å shell density fluctuation times (Figure S2). Sites with longer residence times tend to have longer fluctuations, though the fluctuations are generally fast compared with the residence time; 10 Å density fluctuation times correlate poorly with the residence times due to the presence of faster ions farther out in the shell. It is likely that long-term outer-sphere association sites such as the eight identified here contribute substantially to the enhanced stability of RNA in the presence of Mg^{2+} and modulate kinetics by anchoring their local RNA environments against fluctuations for long times while associated.

3.1.3. Local Mg^{2+} Events Affect Global Dynamics. Since RNA fluctuations occupy the same time scales as Mg^{2+} density fluctuations and Mg^{2+} residence times, they can couple. We now show that Mg^{2+} association in particular sites affects SAM-I conformation and dynamics. Mg^{2+} bridging interactions, in which a single Mg^{2+} mutually attracts phosphates, have been suggested as a mechanism for Mg^{2+} stabilization of tertiary structure.¹⁹ Temporal correlations (eq S4) between individual Mg^{2+} association events and phosphate–phosphate (P–P) distances in the simulations provide evidence for this mechanism (Figure 3). Mg^{2+} association events were modeled by the local ion density about association sites using 10 Å shells as described above.

Correlating time traces of P–P distances with time-dependent local Mg^{2+} densities shows several regions are especially susceptible to Mg^{2+} binding. Mg^{2+} binding within the P4 major groove (C8 to G82 phosphates) shows substantial correlation. When Mg^{2+} enters the P4 major groove, the groove partially closes (Figure 3c), resulting in negative (red) correlations between Mg^{2+} density within the groove and P–

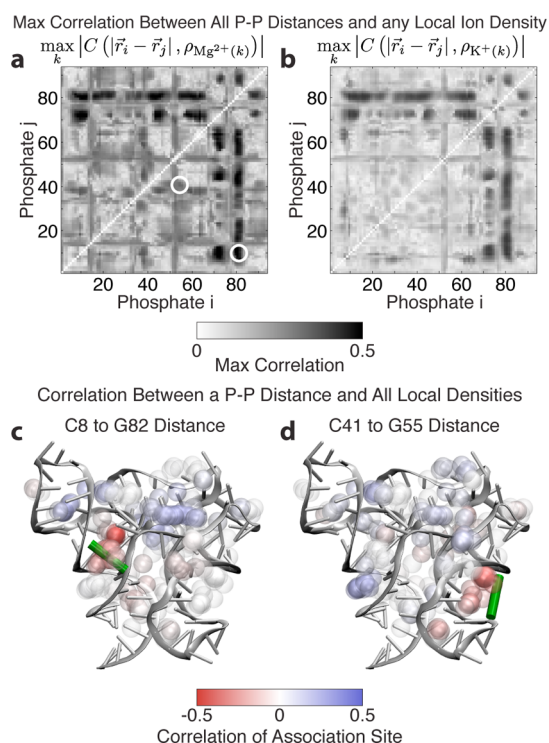


Figure 3. Locally, individual Mg^{2+} association events pull phosphates together by bridging interactions. (a) The correlations between phosphate–phosphate (P–P) distance and the local Mg^{2+} density at the most strongly correlated association site (10 mM simulation). The pairs in panels (c) and (d) are circled. (b) The same plot for K^+ shows lower correlations (0⁺ mM simulation). These correlations represent the passive changes in ionic concentration due to changing RNA structure. (c,d) Two representative P–P distances across a major groove (illustrated by the green bar). The Mg^{2+} density in the groove is negatively correlated (red) because when density in these regions increases, the P–P distance decreases. Balls represent association sites. The density about an association site is computed within a 10 Å shell, but the sites are plotted with a radius of 2.5 Å for clarity, and colored according to their correlation with the P–P distance.

P distance. Several other regions also show strong correlations (Figure 3a), including the P3 groove (C41 to G55 phosphates) (Figure 3d), demonstrating that individual Mg^{2+} association events affect local RNA conformation.

The K^+ correlations in Figure 3b provide a control for the conclusions drawn from the Mg^{2+} correlations in Figure 3a. K^+ fluctuates more than an order of magnitude more quickly than Mg^{2+} , so K^+ cannot couple effectively with RNA motion. The observed correlations between local K^+ density (at the Mg^{2+} sites) and P–P distances are indeed weaker than for Mg^{2+} . They represent K^+ passively responding to the RNA conformation rather than actively modulating it through bridging interactions as Mg^{2+} does.

The effect of Mg^{2+} association events on local RNA conformation in turn affects the global conformation. Correlations were computed between the local density around association sites and the first 25 normal modes. The presence or absence of Mg^{2+} can account for 30–40% of RNA fluctuations along many normal modes (Figure 4a). Several of the lowest and most correlated normal modes are shown with the directions of motion along the normal mode. Normal mode 1 responds to bridging interactions in the P4 major groove (Figure 4b). When Mg^{2+} enters the blue region

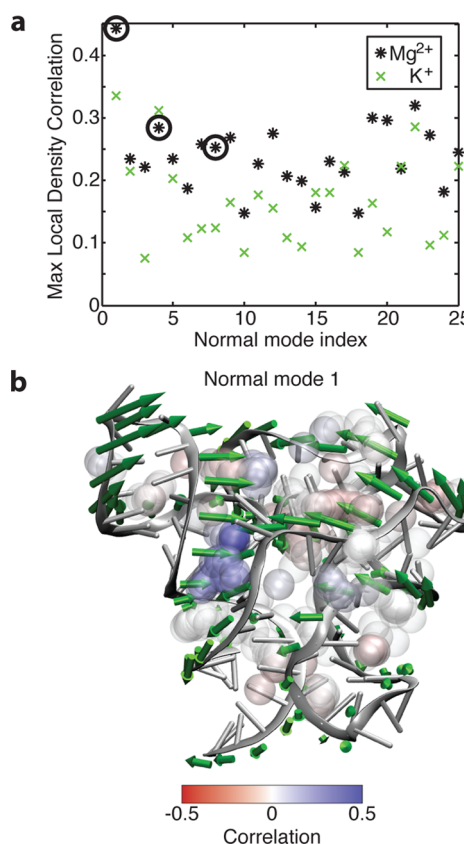


Figure 4. Mg^{2+} association and resulting local bridging interactions also affect the global RNA conformation. (a) Correlations between normal-mode projections and the most strongly correlated local Mg^{2+} density for each normal mode. Several of the first few normal modes are strongly correlated. Circled modes are shown in (b) and in Figure S5. The positive direction of motion along the normal mode is plotted as green arrows. Densities in regions which close upon positive motion along the normal mode are generally positively correlated (blue), while densities in regions which open are generally negatively correlated (red). We note that in the case of the P4 major groove described earlier, positive motion along the normal mode corresponds to a decrease in P–P distance. Thus, a negative correlation between the Mg^{2+} density and the P–P distance corresponds to a positive correlation between the Mg^{2+} density and positive motion along the normal mode. Balls represent association sites and are plotted one-quarter scale as in Figure 3.

(positive correlation), progress along that coordinate increases, and the major groove of P4 surrounding those phosphates closes. (Correlations are opposite from Figure 3c because positive motion along the structural reaction coordinate is in opposite directions.) Normal mode 4 responds to competition between bridging interactions in the P3 and P4 major grooves (Figure S5c). Positive motion along normal mode 4 opens the P4 major groove and closes the P3 major groove, and the resulting correlations are as expected. Normal mode 8 responds to competing bridging interactions on opposite ends of the P4 major groove (Figure S5d). In normal mode 8, the P4 major groove opens on the loop end while closing on the P1 end. Correlations with the association sites in this groove reflect that difference: the loop end displays negative correlations; the P1 end shows positive correlations. Our results show that individual Mg^{2+} association events affect the global conformation by changing local conformation through bridging interactions between phosphates.

Table 1. (Top to Bottom) Number of Ions in Each Simulation, Raw Concentrations Determined 20 Å beyond RNA (asterisk), Concentrations Corrected with a Small Potential Perturbation Approximation, and Preferential Interaction Coefficients Obtained from the Corrected Concentrations

	0 mM	0 [†] mM	1 mM	6 mM	10 mM
$N_{\text{Mg}^{2+}}$	0	1	11	22	33
N_{K^+}	137	133	116	100	84
N_{Cl^-}	45	43	46	52	58
$[\text{Mg}^{2+}]^*$, mM ^a	0.0 ± 0.0	0.0 ± 0.0	1.1 ± 0.9	6.7 ± 2.6	11.2 ± 1.6
$[\text{K}^+]^*$, mM	115.3 ± 2.6	114.2 ± 1.6	113.8 ± 1.9	110.0 ± 4.4	105.5 ± 2.7
$[\text{Cl}^-]^*$, mM	93.1 ± 1.8	90.0 ± 1.1	94.8 ± 1.2	106.5 ± 1.4	115.3 ± 0.7
$[\text{Mg}^{2+}]$, mM ^b	0.0 ± 0.0	0.0 ± 0.0	0.9 ± 0.7	5.8 ± 2.2	10.2 ± 1.4
$[\text{K}^+]$, mM	103.0 ± 2.0	100.6 ± 1.2	102.5 ± 1.7	102.3 ± 4.6	100.5 ± 2.5
$[\text{Cl}^-]$, mM	103.0 ± 2.0	100.6 ± 1.2	104.2 ± 1.1	113.9 ± 1.9	120.8 ± 0.8
$\Gamma_{\text{Mg}^{2+}}$	0.0 ± 0.0	1.0 ± 0.0	10.5 ± 0.4	18.7 ± 1.3	27.2 ± 0.8
Γ_{K^+}	78.0 ± 1.1	75.4 ± 0.7	57.3 ± 1.0	41.4 ± 2.6	26.5 ± 1.5
Γ_{Cl^-}	-14.0 ± 1.1	-14.6 ± 0.7	-13.7 ± 0.6	-13.2 ± 1.1	-11.2 ± 0.5

^aRaw concentration. ^bCorrected concentration $\propto N - \Gamma$.

3.2. Characterization of Outer-Sphere Mg^{2+} .

3.2.1. Ionic Concentrations and Preferential Interaction Coefficients. Since RNA is strongly charged, it attracts excess ions to balance its charge. The excess number of each species of ion i that an RNA molecule attracts into its local environment is called the preferential interaction coefficient Γ_i .¹⁸ Preferential interaction coefficients are of interest because they are experimentally measurable, and allow connection between the simulations and experiment. Electroneutrality requires the preferential interaction coefficients to balance the net RNA charge according to $Z = \sum q_i \Gamma_i$, where Z is the magnitude of the RNA charge and q_i is the charge of each ionic species i .^{52,53} Within this constraint, Γ_i for each species can vary with bulk ionic concentrations due to the availability of various ions.

Simulations were run at several varying concentrations. Table 1 shows the number of ions included in simulations as well as the concentrations and preferential interaction coefficients Γ_i for each species i . The number of ions in the box is the sum of ions contributing to the concentration and the excess ions Γ . Since Γ_i varies with concentration, the number of ions in the box had to be chosen through repeated trials to obtain the desired bulk concentrations. Concentrations as a function of time are computed by counting the number of “bulk” ions, $B_{\text{Mg}^{2+}}$, and water molecules, $B_{\text{H}_2\text{O}}$, more than 20 Å from any RNA atom and taking their ratio. While this technically gives the molality rather than the molarity, we note that the molarity and molality are very close for low ionic concentrations in water. The concentration of an ionic species is given by the time average of the ratio of these molecule counts multiplied by the molarity of pure water.

$$[\text{Mg}^{2+}]^* = 55.51 \text{ M} \frac{B_{\text{Mg}^{2+}}}{B_{\text{H}_2\text{O}}} \quad (1)$$

Since only 95% of the charge is balanced out by 20 Å in 100 mM KCl, the computed concentrations will not sum to zero because some charge density must remain in the rest of the box to balance the residual RNA charge. However, unlike the case near the RNA where ions interact differently with the RNA due to large electrostatic potentials, at 20 Å, the electrostatic potential is a smooth, small perturbation. Ion densities in a

small potential well will respond linearly with their concentration, charge, and the well depth. The corrected bulk concentrations (which must be electroneutral) are given by

$$[i] = [i]^* - q_i [i]^* \frac{\sum_j q_j [j]^*}{\sum_j q_j^2 [j]^*} \quad (2)$$

$$[\text{Mg}^{2+}] = [\text{Mg}^{2+}]^* - 2[\text{Mg}^{2+}]^* \frac{2[\text{Mg}^{2+}]^* + [\text{K}^+]^* - [\text{Cl}^-]^*}{4[\text{Mg}^{2+}]^* + [\text{K}^+]^* - [\text{Cl}^-]^*} \quad (3)$$

where q_i is the charge, $[i]^*$ denotes the raw concentration, and $[i]$ denotes the corrected concentration. If the arbitrary definition of bulk ions as more than 20 Å from the RNA is varied, the corrected concentrations converge much more quickly than the raw concentrations. Once corrected concentrations are obtained, preferential interaction coefficients, Γ , may be computed. Preferential interaction coefficients are the ions in excess of the ions expected from the corrected concentration

$$\Gamma_{\text{Mg}^{2+}} = N_{\text{Mg}^{2+}} - N_{\text{H}_2\text{O}} \frac{[\text{Mg}^{2+}]}{55.51 \text{ M}} \quad (4)$$

where $N_{\text{Mg}^{2+}}$ is the total number of Mg^{2+} ions and $N_{\text{H}_2\text{O}}$ is the total number of water molecules.

Preferential interaction coefficients Γ are experimentally measurable.⁵¹ For a purine riboswitch with 72 residues at 1 mM Mg^{2+} and 50 mM K^+ , $\Gamma_{\text{Mg}^{2+}}$ varies from 13 to 18, depending on mutations and the switch state.^{52,54} We observe a $\Gamma_{\text{Mg}^{2+}}$ of 10.5 at this Mg^{2+} concentration. A lower prediction is expected in the simulation since it has twice as much K^+ competing to balance the RNA charge. There are additional factors that complicate the comparison between experiment and simulation. NMR experiments generally show nearly all K^+ remains fully hydrated, while in most MD simulations (including ours) approximately half of the excess K^+ partially dehydrates and contacts RNA directly.⁵⁵ Our simulations show 40–50% of Γ_{K^+} is partially dehydrated (Figure S11).

We emphasize that our ion parameters produce very stable 2- μ s trajectories. Removal of this population and proportional increase of the remaining populations of excess ions would raise $\Gamma_{\text{Mg}^{2+}}$ for 1 mM Mg^{2+} from 10.5 to 14.7. We note that most of the Mg^{2+} contributing to $\Gamma_{\text{Mg}^{2+}}$ are in the outer-sphere layer of ions, between the inner-sphere and diffuse regimes.

3.2.2. Distance Classes and Diffusion of Mg^{2+} Ions. Mg^{2+} ions can be divided into classes based on distance from RNA^{9,10} (Figure 5a). *Inner-sphere* ions are the closest and make direct

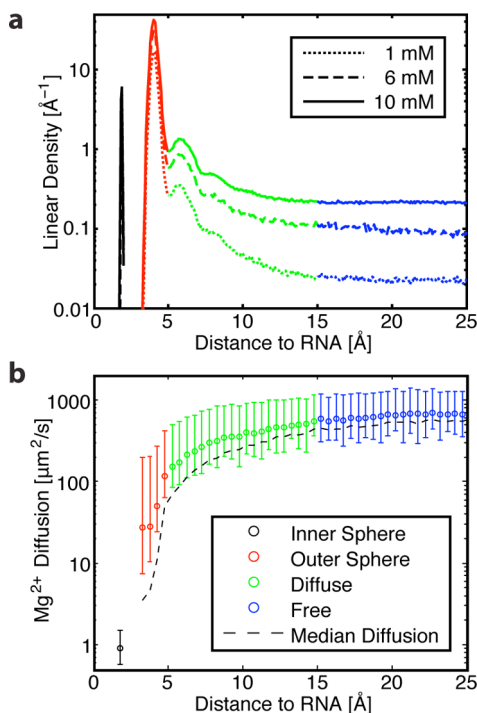


Figure 5. Four classes of Mg^{2+} based on RNA distance emerged during our analysis: *inner-sphere* (black) at 2 $\text{\AA}$, *outer-sphere* (red) at 3–5 $\text{\AA}$, and *diffuse* (green) at 5–15 $\text{\AA}$, blending into *free* (blue). (a) The population of Mg^{2+} as a function of distance from the RNA. The outer-sphere population, which has previously received little attention, composes 80–85% of $\Gamma_{\text{Mg}^{2+}}$ (Table 2). (b) The diffusion of Mg^{2+} as a function of distance from the RNA. Closer Mg^{2+} ions show decreased values of mobility. Bars reflect the variance of instantaneous diffusion above and below the mean. The uncertainty from bootstrap analysis averages approximately 3%. The median instantaneous diffusion is plotted as a dashed line. While the median is comparable to the mean in most regimes, it is substantially below the mean for outer-sphere Mg^{2+} because rare dissociation events dominate the mean. Values are from the 10 mM simulation.

contact with the RNA. Mg^{2+} typically has an octahedral geometry and coordinates with six waters. Each inner-sphere contact with RNA replaces one of these waters. Inner-sphere ions can be further divided into monodentate and chelated ions based on whether they make one or multiple inner-sphere contacts with RNA. The next layer is *outer-sphere*. These Mg^{2+} retain all their inner-sphere waters, and are only separated from the RNA by this single hydration layer. This layer accounts for most of the Mg^{2+} in our simulations, 80–85% of $\Gamma_{\text{Mg}^{2+}}$ (Table 2). Ions in this layer fluctuate on time scales comparable with RNA fluctuations, and couple to the RNA. These Mg^{2+} ions cannot condense closer than this layer without paying substantial dehydration costs. There are several hints that this layer behaves as an ionic glass (section 3.2.4). The next layer is

Table 2. Number and Percentage of Ions in the Distance Classes in Figure 5

	1 mM	6 mM	10 mM
$\Gamma_{\text{Mg}^{2+}}$	10.5	18.7	27.2
Number of Mg^{2+}			
Inner-Sphere ^a	1.0	1.0	1.0
Outer-Sphere	8.6	16.0	22.3
Diffuse	0.9	1.7	3.9
Percent of $\Gamma_{\text{Mg}^{2+}}$			
Inner-Sphere	9.5	5.4	3.7
Outer-Sphere	81.8	85.8	81.8
Diffuse	8.7	8.9	14.5

^aPredicted chelated ions are a subset of the inner-sphere class. Note that the outer-sphere population contains 80–85% of the excess Mg^{2+} ions' $\Gamma_{\text{Mg}^{2+}}$.

diffuse. Diffuse ions are separated from RNA by two or more hydration shells, are poorly ordered, and are well described by continuum models. The farthest group of ions is *free*. The divide between diffuse and free ions is ambiguous. For the present analysis we simply subtract inner-sphere and outer-sphere ions from $\Gamma_{\text{Mg}^{2+}}$. Population enrichment (Figure 5a) and reduced diffusion (Figure 5b) suggest between 10 and 20 $\text{\AA}$ as a reasonable boundary for these two classes.

Diffuse ions are well represented by NLPB distributions due to their low density and rapid dynamics. Outer-sphere ions may be analogous to Manning counterions that condense as close to the RNA as possible and screen its charge. They are dense, have internal correlations, and couple strongly with the RNA. Reasonable thermodynamic agreement with experiment has been obtained by combining a few chelated sites with a NLPB representation of diffuse ions.^{7,8,56} The Tightly Bound Ion method treats outer-sphere ions thermodynamically, resulting in improved calculations of stability.⁶ Our results show that Mg^{2+} also exerts substantial kinetic control. In contexts where RNA kinetics are of interest, the kinetic effects of outer-sphere Mg^{2+} must be carefully considered.

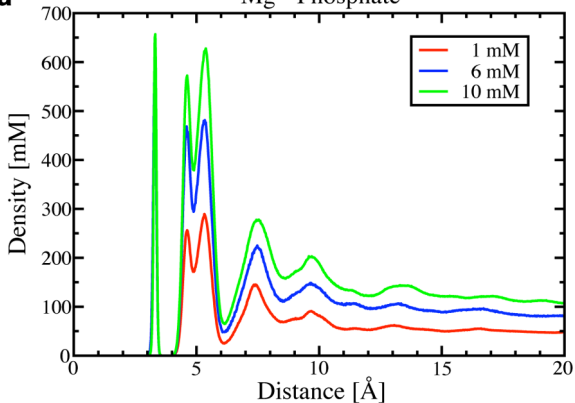
The kinetic effects are highlighted by the different diffusive behavior between Mg^{2+} distance classes (Figure 5b). The diffusion of Mg^{2+} ions was computed as follows. The RNA was first fit to a reference structure, because otherwise the lower Mg^{2+} diffusion values were washed out by the bulk RNA diffusion, which was on the order of 10 $\mu\text{m}^2/\text{s}$. The distance to the nearest RNA heavy atom was found for every frame. The squared displacement for 2 ns periods starting every 200 ps was computed, and then averaged within bins based on starting distance from the RNA. The mean-squared displacement was then fit within each distance bin to $\langle x^2 \rangle = 6Dt$ to obtain diffusion. Instantaneous diffusion could be determined by fitting the mean-squared displacement before averaging within distance bins.

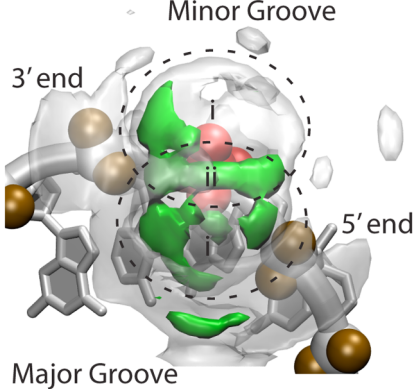
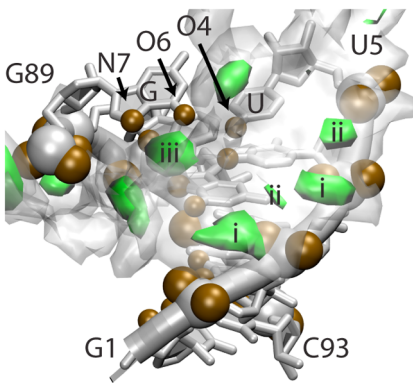
The Mg^{2+} ion in the inner-sphere class has the lowest diffusion. This ion does not move relative to the RNA during the simulation, so its diffusion is nearly zero, and the plotted value of 1 $\mu\text{m}^2/\text{s}$ indicates our method's precision. The outer-sphere Mg^{2+} ions have a diffusion coefficient (20–30 $\mu\text{m}^2/\text{s}$) roughly 2 orders of magnitude below bulk. As mentioned before, outer-sphere ions account for most of the Mg^{2+} associated with the RNA. Depending on the site, they can remain associated from a few to several thousand nanoseconds.

Due to heterogeneous sites, glassy dynamics, and escape to regions with higher diffusion, the diffusion of the inner-sphere

a

Mg - Phosphate



a**b**

region of intermediate mobility between inner-sphere and diffuse, which allows them to couple to the RNA.

Previously, the interplay between Mg^{2+} and RNA has frequently been modeled by chelation sites and a diffuse ion cloud. Diffuse ions are well represented by NLPB distributions due to their low density and rapid dynamics. In contrast, outer-sphere ions may be more reminiscent of Manning counterions that condense as close to the RNA as possible. Our simulations include explicitly discrete ion effects, internal correlations, and kinetic coupling between outer-sphere Mg^{2+} and the RNA. Since outer-sphere Mg^{2+} are the dominant population and have a substantial effect on RNA dynamics, we propose a new view of Mg^{2+} –RNA interactions where the outer-sphere Mg^{2+} class, with glass-like internal correlations, both thermodynamically stabilizes and exerts kinetic control on RNA. Future reduced treatments of Mg^{2+} –RNA interactions need to consider the importance of the inherently discrete ion effects of the outer-sphere Mg^{2+} .

■ ASSOCIATED CONTENT

■ Supporting Information

Details of normal-mode calculation and comparison of the normal modes to the principal components; additional time scale and autocorrelation data; 3D representation of association sites and residence times; association site correlations with two additional normal modes; RMSF of RNA by residue; the K^+ populations as a function of distance from RNA; methods for autocorrelation and correlation computations; details about the predicted chelated Mg^{2+} ion; and a movie of the equilibration procedure. This material is available free of charge via the Internet at <http://pubs.acs.org>.

■ AUTHOR INFORMATION

Corresponding Author

kys@lanl.gov

Notes

The authors declare no competing financial interest.

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